

Wide binaries as a critical test for Gravity theories

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Abstract. Assuming Newton's gravity and GR to be valid at all scales leads to the dark matter hypothesis as a requirement demanded by the observed dynamics and measured baryonic content at galactic and extragalactic scales. Alternatively, modified gravity scenarios where a change of regime appears at acceleration scales $a < a_0$ have been proposed. This modified regime at $a < a_0$ will generically be characterised by equilibrium velocities which become independent of distance. Here we identify a critical test in this debate and we propose its application to samples of wide binary stars. Since for $1M_\odot$ systems the acceleration drops below a_0 at scales of around 7000 AU, a statistical survey of wide binaries with relative velocities and separations reaching 10^4 AU and beyond should prove useful to the above debate. We apply the proposed test to the best currently available data. Results show a constant upper limit to the relative velocities in wide binaries which is independent of separation for over three orders of magnitude, in analogy with galactic flat rotation curves in the same $a < a_0$ acceleration regime. Our results are suggestive of a breakdown of Kepler's third law beyond $a \approx a_0$ scales, in accordance with generic predictions of modified gravity theories designed not to require any dark matter at galactic scales and beyond.

1. Introduction

Over the past years the dominant explanation for the large mass to light ratios inferred for galactic and meta-galactic systems, that these are embedded within massive dark matter halos, has begun to be challenged. Direct detection of the dark matter particles, in spite of decades of extensive and dedicated searches, remains lacking. Numerous alternative theories of gravity have appeared (e.g. TeVeS of [1], F(R) theories e.g. [8]) mostly grounded on geometrical extensions to General Relativity, and leading to laws of gravity which in the low acceleration regime, mimic the MODified Newtonian Dynamics (MOND) fitting formulas e.g. [7]. Similarly, [6] have explored MOND not as a modification to Newton's second law, but as a modified gravitational force law in the Newtonian regime, finding a good agreement with observed dynamics across galactic scales without requiring dark matter. Recently [2] have constructed an $f(R)$ extension to general relativity which in the low velocity limit converges to the above approach.

A generic feature of all such modified gravity schemes is the appearance of an acceleration scale, a_0 , above which classical gravity is recovered, and below which the dark matter mimicking regime appears. This results in a general prediction; all systems where $a \gg a_0$ should appear as devoid of dark matter, and all systems where $a \ll a_0$ should appear as dark matter dominated. It is interesting that no $a \gg a_0$ system has ever been detected where dark matter needs to be invoked. On the other hand, the latter condition furnishes a testable prediction in relation to the orbits of wide binaries. For test particles in orbit around a $1M_\odot$ star, in circular orbits

of radius s , the acceleration is expected to drop below $a_0 \approx 1.2 \times 10^{-10} m/s^2$ for $s > 7000$ AU = $3.4 \times 10^{-2} pc$. This provides a test for the dark matter/modified theories of gravity debate; the relative velocities of components of binary stars with large physical separations should deviate from Kepler's third law. Seen as an equivalent Newtonian force law, beyond $s \approx 7000$ AU the gravitational force should gradually switch from the classical form of $F_N = GM/s^2$ to $F_{MG} = (GMa_0)^{1/2}/s$, and the orbital velocity, $V^2/s = F$, should no longer decrease with separation, but settle at a constant value, dependent only on the total mass of the system through $V = (GMa_0)^{1/4}$. Under modified gravity theories, binary stars with separations beyond 7000 AU should exhibit "flat rotation curves" and a "Tully-Fisher relation", as galactic systems in the same acceleration regime do.

We apply this test to the binaries of two recent catalogues containing relative velocities and separations. The two catalogues are entirely independent in their approaches. The first one, [8], comprises 280 systems from the *Hipparcos* satellite, while the second, [3], identifies 1,250 ones from the Sloan Digital Sky Survey (SDSS). Details can be found in [4].

2. Relative velocity distributions for wide binaries under Newtonian expectations

The Newtonian prediction for the relative velocities of the two components of binaries having circular orbits, when plotted against the binary physical separation, s , is for a scaling of $\Delta V \propto s^{-1/2}$, essentially following Kepler's third law, provided the range of masses involved were narrow. In a relative proper motion sample however, only two components of the relative velocity appear, as velocity along the line of sight to the binary leads to no proper motion. Thus, orbital projection plays a part, with systems having orbital planes along the line of sight sometimes appearing as having no relative proper motions. A further effect comes from any degree of orbital ellipticity present; it is hence clear that the trend for $\Delta V \propto s^{-1/2}$ described above, will only provide an upper limit to the distribution of projected ΔV vs. s expected in any real observed sample, even if only a narrow range of masses is included. One should expect a range of measured values of projected ΔV at a fixed observed projected s , all extending below the Newtonian limit, which for equal mass binaries in circular orbits gives $\Delta V_N = 2 \left(\frac{GM}{s} \right)^{1/2}$.

Further, over time, the orbital parameters of binaries will evolve due to the effects of Galactic tidal forces and dynamical encounters with other stars in the field, specially in the case of wide binaries. To first order, one would expect little evolution for binaries tighter than the tidal limit of 1.7 pc, and the eventual dissolution of wider systems. A very detailed study of all these points has recently appeared, [5]. These authors numerically follow populations of 50,000 $1M_\odot$ binaries in the Galactic environment, accounting for the evolution of the orbital parameters of each due to the cumulative effects of the Galactic tidal field at the Solar radius. Also, the effects of close and long range encounters with other stars in the field are carefully included, to yield a present day distribution of separations and relative velocities for an extensive population of wide binaries, under Newtonian Gravity.

It is found that when many wide binaries cross their Jacobi radius, the two components remain fairly close by in both coordinate and velocity space. Thus, in any real wide binary search a number of wide pairs with separations larger than their Jacobi radii will appear. Finally, [5] obtain the RMS one-dimensional relative velocity difference, ΔV_{1D} , projected along a line of sight, for the entire populations of binaries dynamically evolved over 10 Gyr to today, as plotted against the projected separation on the sky for each pair. The expected Keplerian fall of $\Delta V_{1D} \propto s^{-1/2}$ for separations below 1.7 pc is obtained, followed by a slight rise in ΔV_{1D} as wide systems cross the Jacobi radius threshold. ΔV_{1D} then settles at RMS values of $\approx 0.1 km/s$. This represents the best currently available estimate of how relative velocities should scale with projected separations for binary stars (both bound and in the process of dissolving in the Galactic tides) under Newtonian gravity. We see that all we need is a large sample of relative

proper motion and binary separation measurements to test the Newtonian prediction for the RMS values of the 1 dimensional relative velocities of [5], and to contrast the $\Delta V_N \propto s^{-1/2}$ and the $\Delta V_{MG} = cte.$ predictions for the upper envelope of the ΔV vs. s distributions.

3. Observed wide binary Samples

In the [8] catalogue wide binaries are identified by assigning a probability above chance alignment to the systems by carefully comparing to the underlying background (and its variations) in a 5 dimensional parameter space of proper motions and spatial positions. We keep only binaries with a probability of non-chance alignment greater than 0.9. The binary search criteria used by the authors requires that the proposed binary should have no near neighbours; the projected separation between the two components is thus always many times smaller than the typical interstellar separation. We use the reported distances to the primaries, where errors are smallest, to calculate projected ΔV and projected s from the measured $\Delta\mu$ and $\Delta\theta$ values reported. Although the use of *Hipparcos* measurements guarantees the best available quality in the data, we have also removed all binaries for which the final signal to noise ratio in the relative velocities was lower than 0.3.

We are left with a sample of 280 binaries, having distances to the Sun within $6 < d < 100$ in pc. The data show a perfectly flat upper envelope in a ΔV vs. projected s , [4]. The average signal to noise ratio for the data is 1.7, with an average error on ΔV of 0.83 km/s , which considering a 2σ factor from the top of the distribution to the real underlying upper limit for the sample, results in 3 km/s as our estimate of the actual physical upper limit in ΔV .

The Sloan low mass wide pairs catalogue (SLoWPoKES) of [3] contains a little over 1,200 wide binaries with relative proper motions for each pair, distances and angular separations. Also, extreme care was taken to include only physical binaries, with a full galactic population model used to exclude chance alignment stars using galactic coordinates and galactic velocities, resulting in an estimate of fewer than 2% of false positives. This yields only isolated binaries with no neighbours within many times the internal binary separation. Again, we use the reported distances to the primaries to calculate projected ΔV and projected s from the measured $\Delta\mu$, $\Delta\theta$ and d values reported by [3], to obtain a sample of 417 binaries.

The upper envelope of the distribution of ΔV from this catalogue does not comply with Kepler's third law. As was the case with the *Hipparcos* sample, the upper envelope describes a flat line, as expected under modified gravity schemes. The average signal to noise in ΔV for the [3] catalogue is 0.48, with an average error on ΔV of 12 km/s , which considering a 2σ factor from the top of the complete distribution to the real underlying upper limit gives the same 3 km/s as obtained for the [8] *Hipparcos* catalogue.

Figure (1) shows the RMS value of the one-dimensional relative velocity difference for both of the samples discussed. The error bars give the error propagation on $\Delta\mu$ and d . We construct ΔV_{1D} by considering only one coordinate of the two available from the relative motion on the plane of the sky. Thus, each binary can furnish two ΔV_{1D} measurements, which statistically should not introduce any bias. Indeed, using only $\Delta\mu_l$ or only $\Delta\mu_b$ or both for each binary, yields the same mean values for the points shown. The small solid error bars result from considering an enlarged sample where each binary contributes two ΔV_{1D} measurements, while the larger dotted ones come from considering each binary only once, and do not change if we consider only $\Delta\mu_l$ or only $\Delta\mu_b$. The series of small $\log(s)$ interval data are for the *Hipparcos* catalogue of [8], while the two broader crosses show results for the [3] SDSS sample.

The solid curve is the Newtonian prediction of the full Galactic evolutionary model of [5] for binaries, both bound and in the process of dissolving. Note that the results of this simulation deviate from Kepler's law for s larger than the Newtonian Jacobi radius of 1.7 pc , whereas the discrepancy with the observed samples also occurs at much smaller separations. Even considering the large error bars, where each binary contributes only one ΔV_{1D} value, we see eight points lying

beyond 1σ , making the probability of consistency between this prediction and the observations of less than $(0.272)^8 = 3 \times 10^{-5}$.

We obtain a constant RMS value for ΔV_{1D} of 1 km/s , in qualitative agreement with expectations from modified gravity schemes. The vertical line marks $a = a_0$; we see the data departing from the Newtonian prediction outwards of this line, and not before. The two independent catalogues, each using different sets of selection criteria, each perhaps subject to its own independent systematics, are consistent with the same result, a constant horizontal upper envelope for the distribution of relative velocities on the plane of the sky at an intrinsic value of $3 \text{ km/s} \pm 1 \text{ km/s}$, extending over 3 orders of magnitude in s , with a constant RMS ΔV_{1D} value consistent with $1 \text{ km/s} \pm 0.5 \text{ km/s}$. This supports the interpretation of the effect detected as the generic prediction of modified gravity theories.

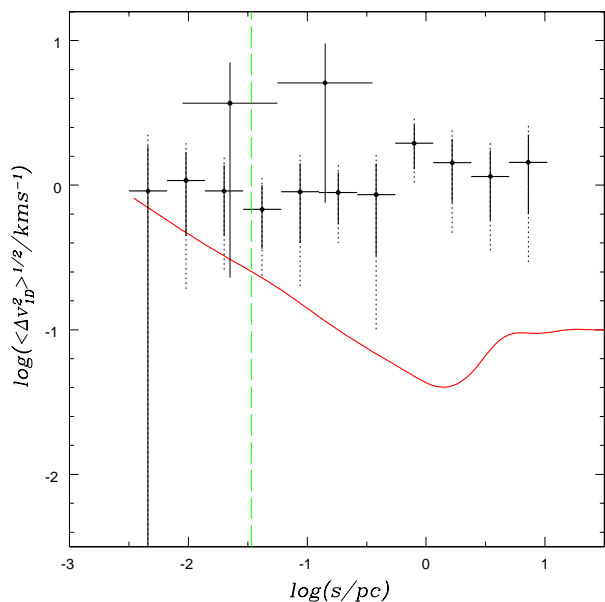


Figure 1. The solid curve gives the RMS values for one dimensional projected relative velocities as a function of projected separations, for the dynamical modelling of large populations of wide binaries evolving in the Galactic environment, taken from [5]. The same quantity for the data from the catalogues analysed is given by the points with error bars; those with narrow $\log(s)$ intervals being from the *Hipparcos* sample of [8], and those two with wide $\log(s)$ intervals coming from the SDSS sample of [3]

4. Conclusions

We identify a critical test in the classical gravity/modified gravity debate, using the relative velocities of wide binaries with separations in excess of 7000 AU, as these occupy the $a < a_0$ regime. We present a first application of this test using the best currently available data. Results show constant relative RMS velocities for the binary stars in question. This is quantitatively inconsistent with detailed predictions of Newtonian dynamical models for binaries evolving in the local galactic environment. Our results are qualitatively in accordance with generic modified gravity models which explain galactic dynamics in the absence of dark matter.

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